



# Comparison of Virtual Network Embedding Algorithms for Data Center Networks

Hardeep Kaur Takhar, Ana Laura Gonzalez Rios,  
and Ljiljana Trajković

Simon Fraser University

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Communication Networks Laboratory  
<http://www.ensc.sfu.ca/~ljilja/cnl/>  
Simon Fraser University  
Vancouver, British Columbia, Canada

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# Roadmap

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- Introduction
- Virtual network embedding
- Data center network topologies
- Simulation scenarios and results
- Conclusion
- References

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# Data centers

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<https://www.google.com/about/datacenters/gallery/#!//%23gallery>

# Data center networks virtualization

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- **Virtualization in data center networks:**
  - reduces inefficient resource utilization and addresses high storage and processing demands
  - enables flexible network operability and maintenance by sharing the existing physical network resources
- **Software defined network model:**
  - decouples the network layer control and data planes
  - leads to logically centralized approach that facilitates network management

# Virtualized network model

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- **Network virtualization:**
  - Two types: infrastructure (InPs) and service (SPs) providers
- **Virtual network embedding (VNE):**
  - process of embedding virtual networks (VNs) onto substrate networks (SNs)
    - virtual node mapping (VNoM)
    - virtual link mapping (VLiM)
  - NP-hard problem with a large solution space
  - a crucial component in the VNE process is attending to virtual network requests (VNRs) with variable arrival rates

# Roadmap

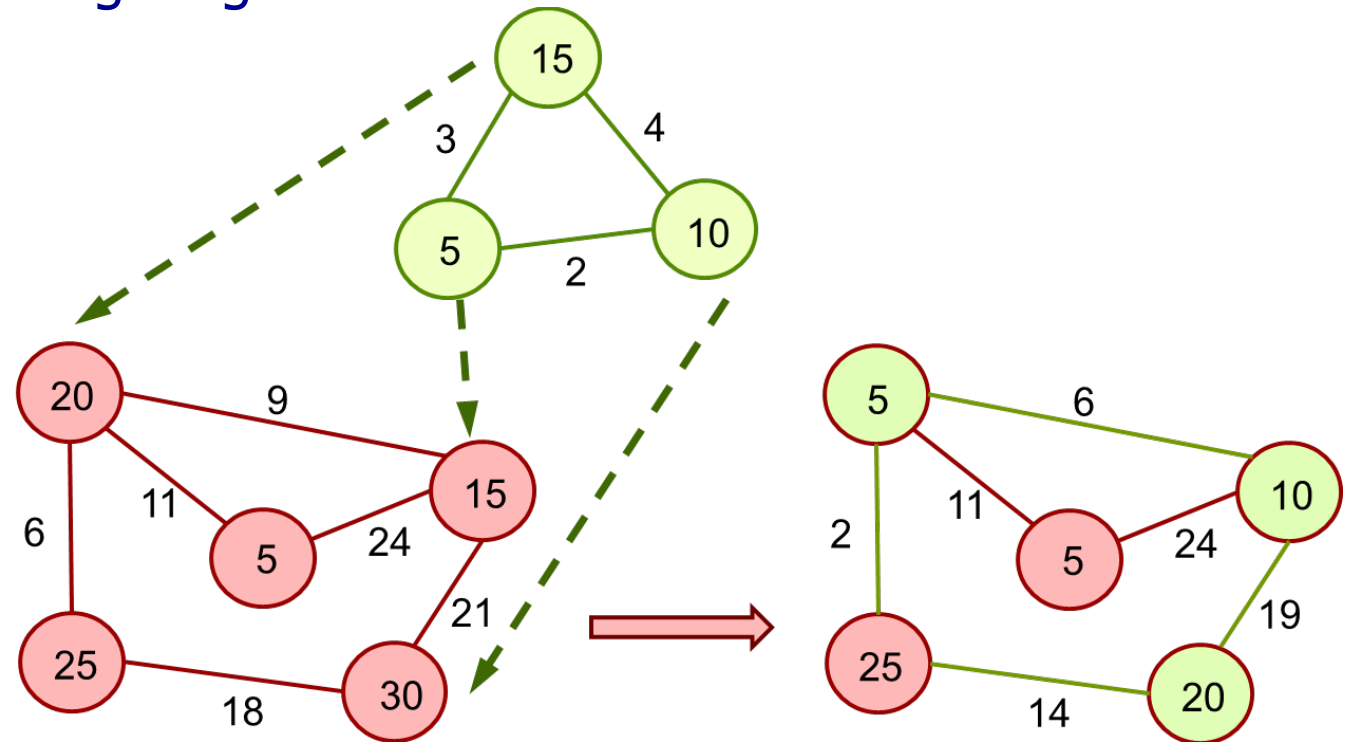
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# Virtual network embedding

- VNE problem may be solved by employing:
  - heuristic uncoordinated algorithms
  - coordination between embedding stages



# VNE approaches: uncoordinated

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- Uncoordinated two-stage algorithms solve:
  - VNoM:
    - heuristic
  - VLiM:
    - Shortest Path: without path splitting
    - Multi-Commodity Flow: with path splitting
  - Restricted solution space: algorithms ignore preselection of node mappings

VNoM: Virtual Node Mapping  
VLiM: Virtual Link Mapping  
SP: Shortest Path  
MCF: Multi-Commodity Flow

# VNE algorithms: coordinated

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- The coordinated two-stage algorithms solve:
  - VNoM first while considering link constraints and availability
  - VLiM then employs SP or MCF techniques
- The coordinated one-stage algorithms:
  - simultaneously solved by creating a suitable optimal virtual link between the nodes

Y. Zhou, Y. Li, D. Jin, L. Su, and L. Zeng, "A virtual network embedding scheme with two-stage node mapping based on physical resource migration," in *Proc. IEEE Int. Conf. Commun. Syst.*, Singapore, Nov. 2010, pp. 761–766.

H. Yu, V. Anand, C. Qiao, H. Di, and X. Wei, "A cost efficient design of virtual infrastructures with joint node and link mapping," *J. Netw. Syst. Manage.*, vol. 20, no. 1, pp. 97–115, Sept. 2012.

# Virtual networks embedding

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Evaluated algorithms:

- Monte Carlo Tree Search (MCTS)-based:
  - Multi-Commodity Flow (MaVEn-M)
  - Shortest path (MaVEn-S)
- Deterministic (D-ViNE) and Randomized (R-ViNE)
- Global Resource Capacity (GRC)
- GRC with Multi-Commodity Flow (GRC-M)

# Coordinated virtual networks embedding

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- MCTS-based Multi-Commodity Flow (**MaVEn-M**):
  - coordinates stages and embeds virtual links using MCF
- MCTS-based shortest path (**MaVEn-S**):
  - employs breadth first search to coordinate stages and to embed virtual links
- Global Resource Capacity Multi-Commodity Flow (**GRC-M**):
  - improves substrate resources utilization by allowing path splitting

S. Haeri and Lj. Trajkovic, "Virtual network embedding via Monte-Carlo tree search," *IEEE Transactions on Cybernetics*, vol. 47, no. 2, pp. 1–12, Feb. 2017.

S. Haeri, Q. Ding, Z. Li, and Lj. Trajković, "Global resource capacity algorithm with path splitting for virtual network embedding," in *Proc. IEEE Int. Symp. Circuits and Systems*, Montreal, Canada, May 2016, pp. 666–669.

# Coordinated virtual networks embedding

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- ViNEYard:
  - deterministic: D-ViNE
  - randomized: R-ViNE
- Global Resource Capacity: GRC
  - nodes sorted based on GRC
  - embedded using greedy algorithms

M. Chowdhury, M. R. Rahman, and R. Boutaba, “ViNEYard: Virtual network embedding algorithms with coordinated node and link mapping,” *IEEE/ACM Trans. Netw.*, vol. 20, no. 1, pp. 206–219, Feb. 2012.

L. Gong, Y. Wen, Z. Zhu, and T. Lee, “Toward profit-seeking virtual network embedding algorithm via global resource capacity,” in *Proc. IEEE INFOCOM*, Toronto, ON, Canada, Apr. 2014, pp. 1–9.

# Performance metrics

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- Virtual network request acceptance ratio
- Generated revenue
- Cost of mapping nodes and links
- Substrate resource utilization

# Performance metrics: VNR acceptance ratio

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- Accepted requests:

$$p_a^\tau = \frac{|\Psi^a(\tau)|}{|\Psi(\tau)|}$$

- $|\Psi^a(\tau)|$ : number of accepted VNRs in a given time interval  $\tau$
- $|\Psi(\tau)|$ : number of all arrived VNRs in time slot  $\tau$
- Goal: maximize acceptance ratio

VNR: Virtual network request



# Performance metrics: generated revenue

- Revenue generated by embedding VNR  $\Psi_i$  :

$$\mathbf{R}(G^{\Psi_i}) = w_c \sum_{n^{\Psi_i} \in N^{\Psi_i}} \mathcal{C}(n^{\Psi_i}) + w_b \sum_{e^{\Psi_i} \in E^{\Psi_i}} \mathcal{B}(e^{\Psi_i})$$

- $G^{\Psi_i}(N^{\Psi_i}, E^{\Psi_i})$ : graph of the  $i^{th}$  virtual network request
- $w_c$  and  $w_b$  : weights for CPU and bandwidth requests
- $n^{\Psi_i}$  and  $e^{\Psi_i}$ : virtual nodes and links
- $\mathcal{C}(n^{\Psi_i})$  and  $\mathcal{B}(e^{\Psi_i})$ : CPU and bandwidth requirements
- Assumption:  $w_c = w_b = 1$
- Goal: maximize revenue

# Performance metrics: incurred cost

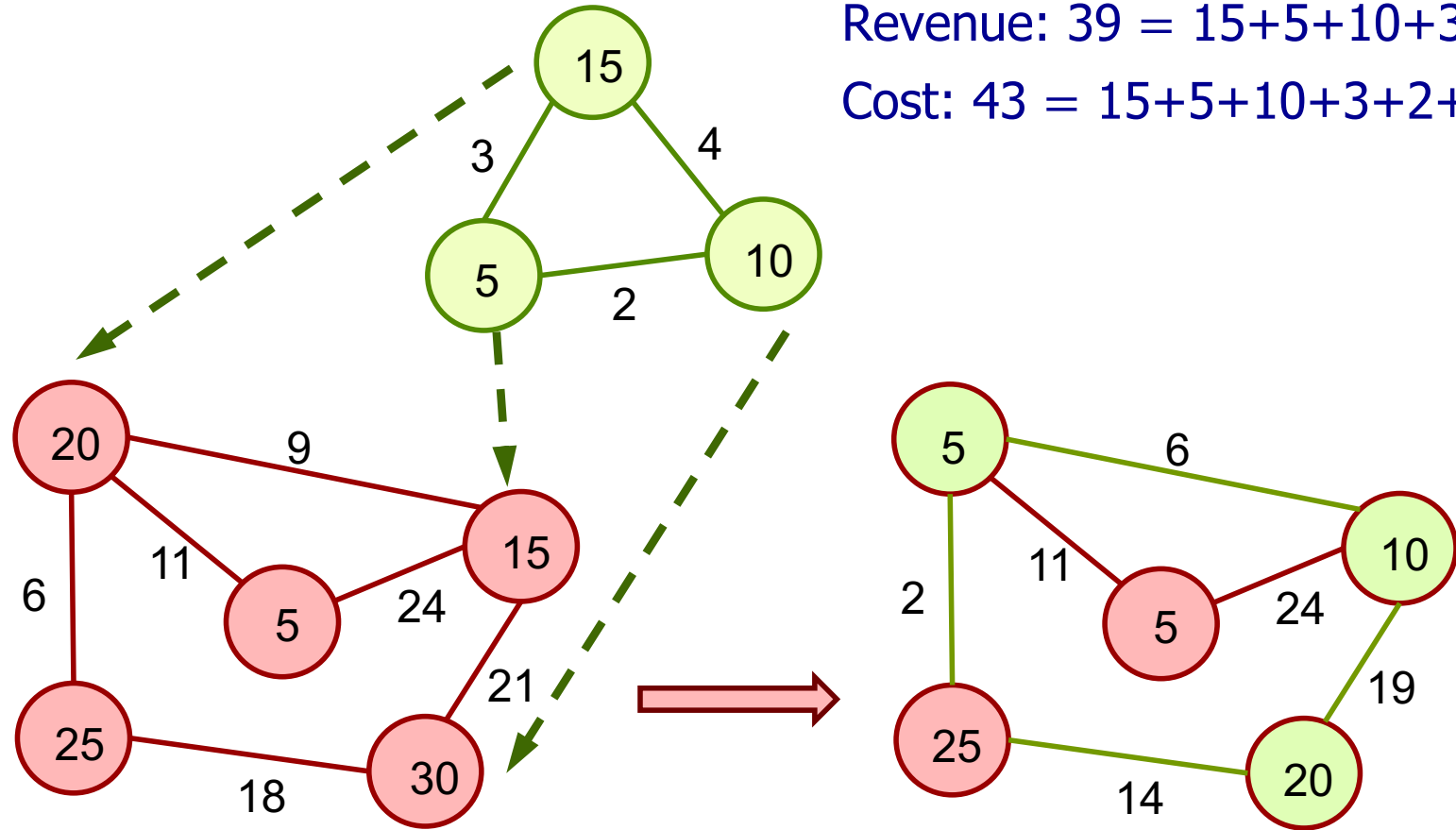
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- Cost of embedding configuration and allocating substrate resources:

$$\mathbf{C}(G^{\Psi_i}) = \sum_{n^{\Psi_i} \in N^{\Psi_i}} \mathcal{C}(n^{\Psi_i}) + \sum_{e^{\Psi_i} \in E^{\Psi_i}} \sum_{e^s \in E^s} f_{e^s}^{e^{\Psi_i}}$$

- $f_{e^s}^{e^{\Psi_i}}$  : total bandwidth of substrate link  $e^s$  allocated to the virtual link  $e^{\Psi_i}$
  - $\mathcal{C}(n^{\Psi_i})$ : CPU requirements
- Goal: minimize the cost

# VNE: example



Revenue:  $39 = 15+5+10+3+2+4$

Cost:  $43 = 15+5+10+3+2+4+4$

# Performance metrics: node utilization

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- Substrate node utilization:

$$\mathcal{U}(N^s) = 1 - \frac{\sum_{n^s \in N^s} \mathcal{C}(n^s)}{\sum_{n^s \in N^s} \mathcal{C}_{max}(n^s)}$$

- $\mathcal{C}(n^s)$ : available CPU resource of substrate node
  - $\mathcal{C}_{max}(n^s)$ : maximum CPU resource of the node
- Goal: optimize the node utilization

# Performance metrics: link utilization

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- Substrate link utilization:

$$\mathcal{U}(E^s) = 1 - \frac{\sum_{e^s \in E^s} \mathcal{B}(e^s)}{\sum_{e^s \in E^s} \mathcal{B}_{max}(e^s)}$$

- $\mathcal{B}(e^s)$ : available bandwidth of substrate link
  - $\mathcal{B}_{max}(e^s)$ : maximum bandwidth of the link
- 
- Goal: optimize the link utilization

# Roadmap

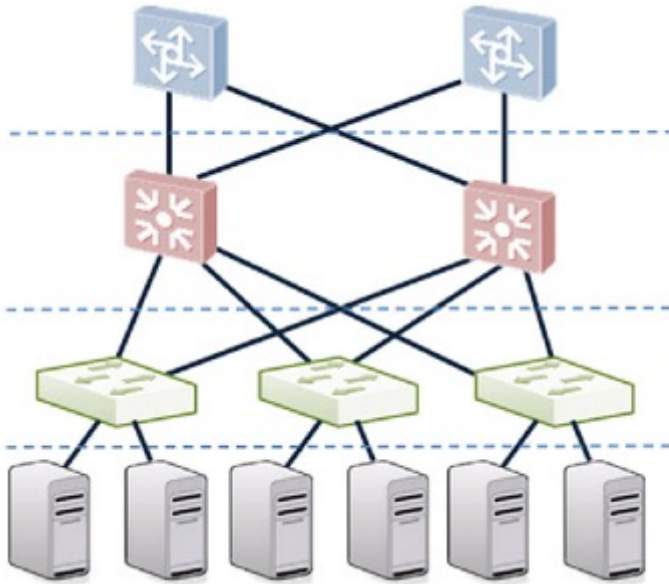
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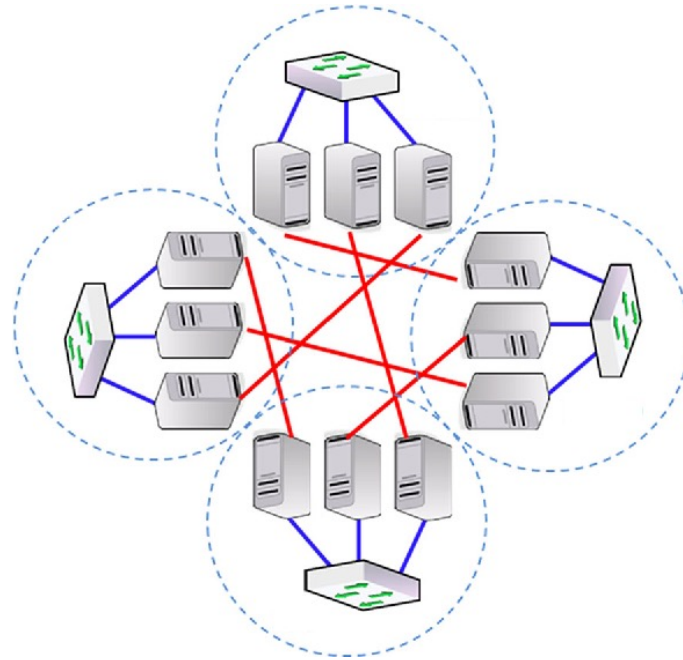
# Data center topologies

- Classified based on the implementation of packet forwarding:

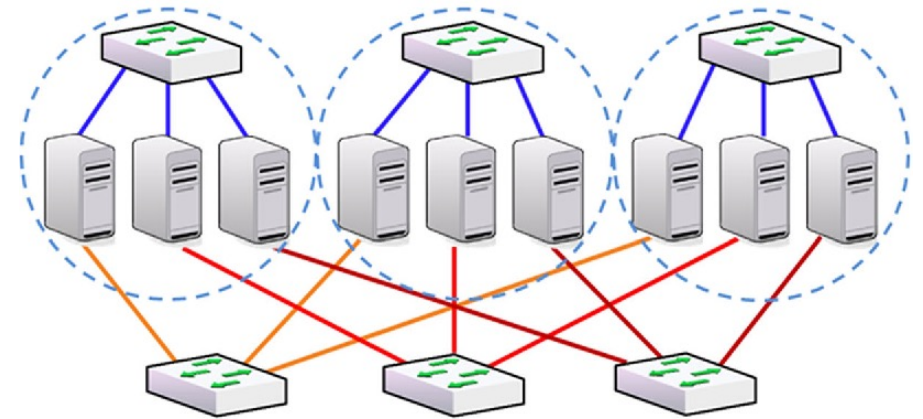
switch-centric



server-centric



hybrid



W. Xia, P. Zhao, Y. Wen, and H. Xie, "A survey on data center networking (DCN): infrastructure and operations," *IEEE Commun. Surveys Tuts.*, vol. 19, no. 1, pp. 640–656, First Quarter 2017

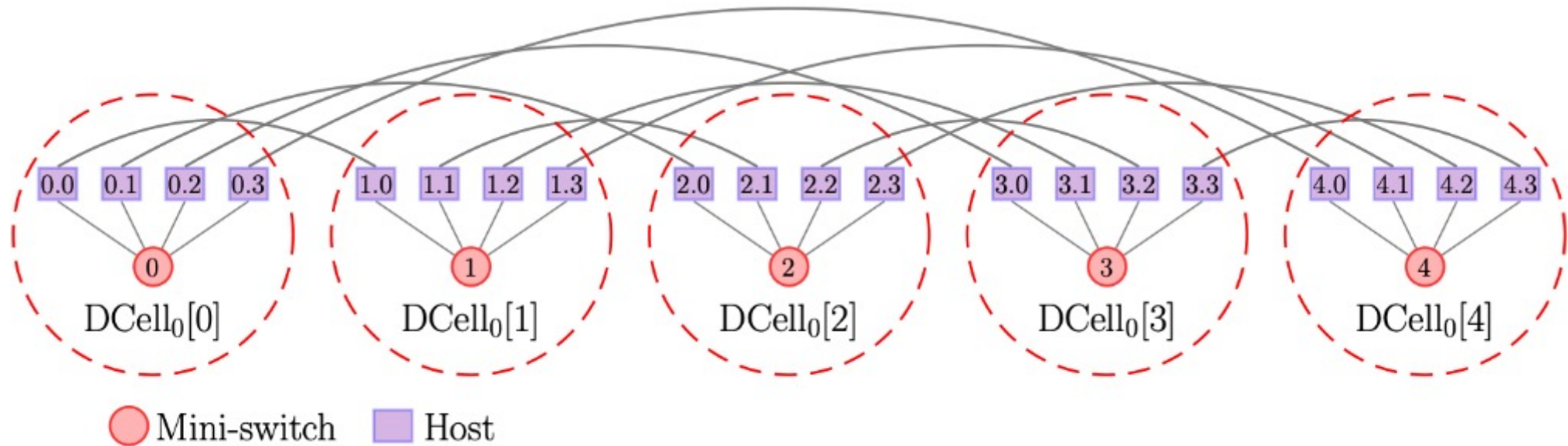
# Data center network topologies

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- Switch-Centric:
  - Fat-Tree
  - F<sup>2</sup>Tree
  - Diamond
  - Spine-Leaf
  - Three-Tier
  - Collapsed Core
- Server-Centric:
  - BCube
  - DCell
  - FiConn
  - Crystal
- Hybrid:
  - Star-wired ring

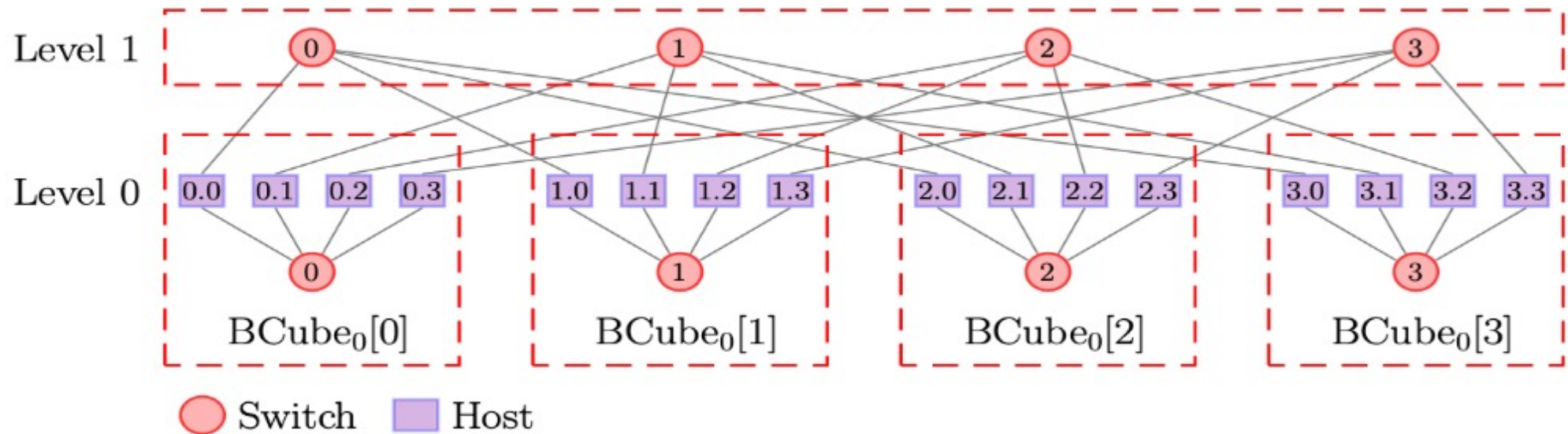


# Server-centric topologies: DCell



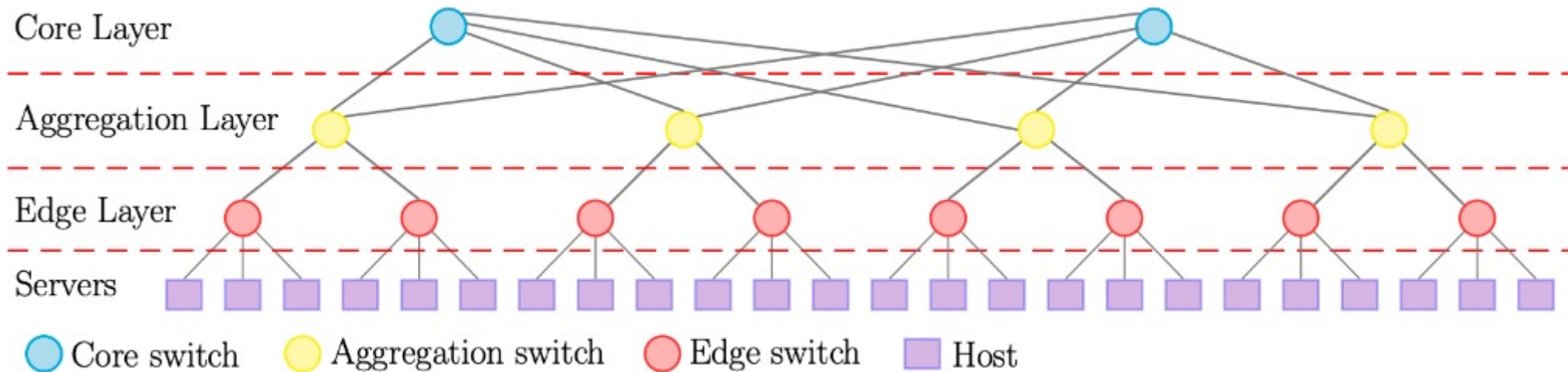
C. Guo, H. Wu, K. Tan, L. Shi, Y. Zhang, and S. Lu, "DCell: a scalable and fault-tolerant network structure for data centers," in *Proc. ACM SIGCOMM*, Seattle, WA, USA, Aug. 2008, pp. 75–86.

# Server-centric topologies: BCube



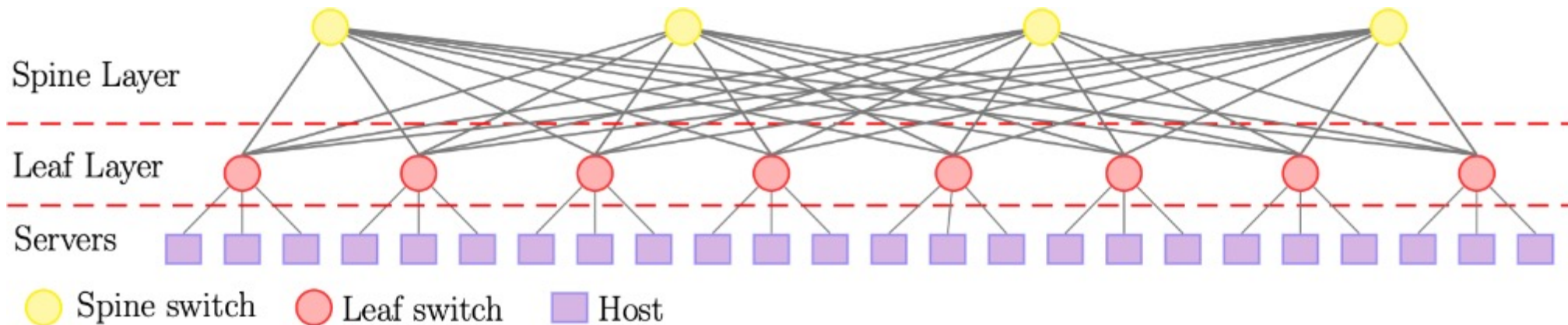
C. Guo, G. Lu, D. Li, H. Wu, X. Zhang, Y. Shi, C. Tian, Y. Zhang, and S. Lu, "BCube: a high performance, server-centric network architecture for modular data centers," *ACM SIGCOMM Comput. Commun. Rev.*, vol. 39, no. 4, pp. 63–74, Oct. 2009.

# Switch-centric topologies: Three-Tier



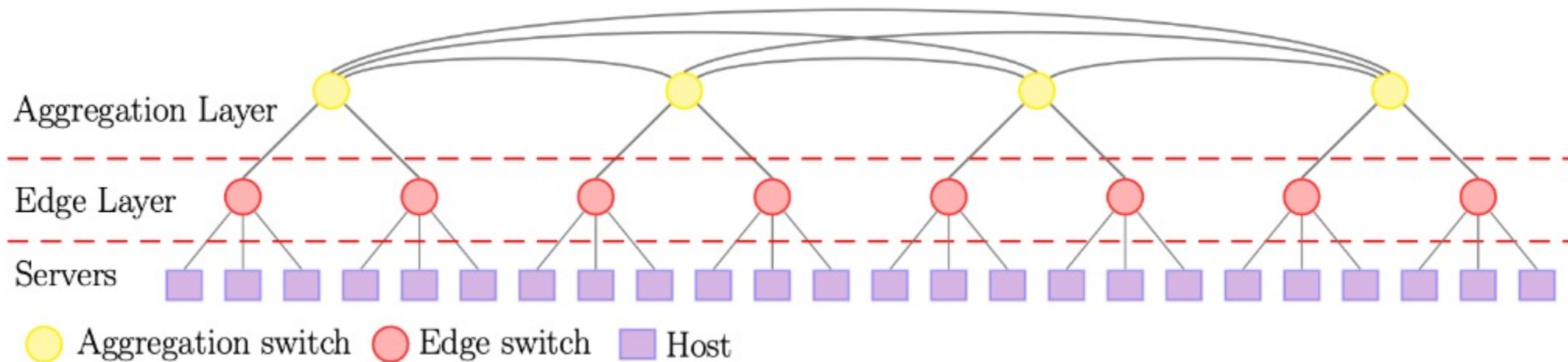
N. Grozev and R. Buyya, "Multi-cloud provisioning and load distribution for three-tier applications," *ACM Trans. Auton. Adapt. Syst.*, vol. 9, pp. 1–21, July 2014.

# Switch-centric topologies: Spine-Leaf (Leaf-Spine)



M. Alizadeh and T. Edsall, "On the data path performance of leaf-spine datacenter fabrics," in *Proc. IEEE 21st Annu. Symp. High-Perform. Interconnects*, San Jose, CA, Aug. 2013, pp. 71–74.

# Switch-centric topologies: Collapsed Core



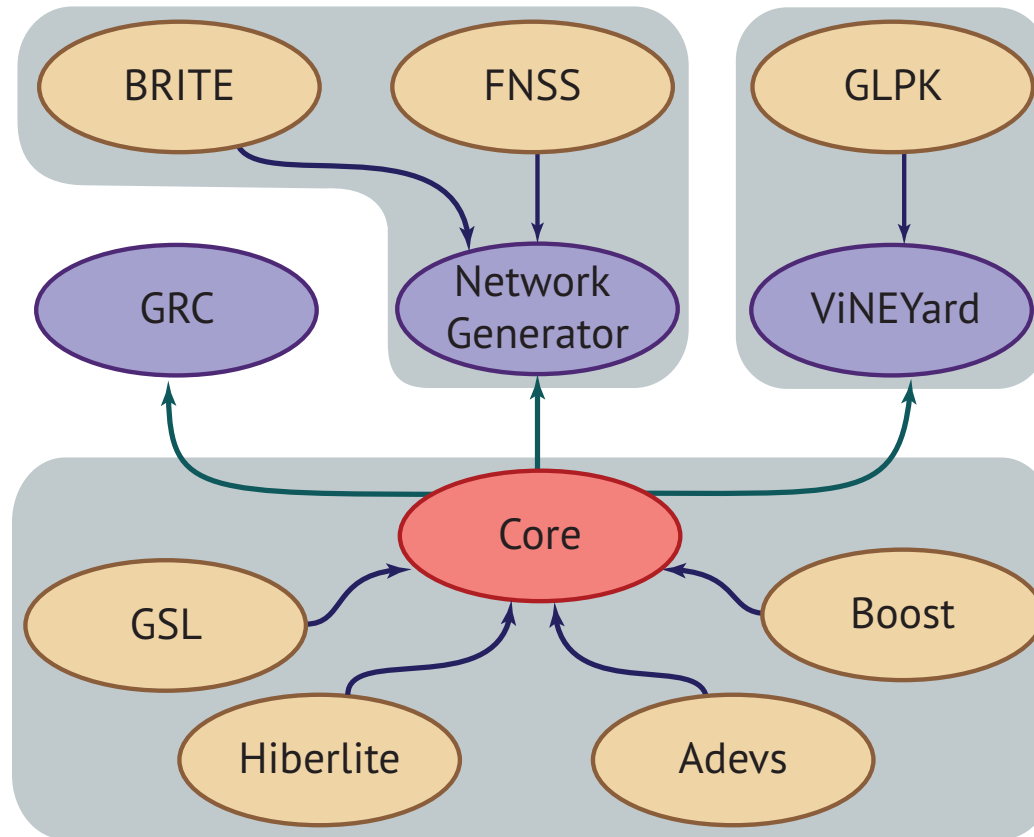
Small enterprise design profile reference guide, Cisco. [Online]. Available: <https://www.cisco.com/c/en/us/td/docs/solutions/Enterprise/Small Enterprise Design Profile/SEDP.html>. Accessed: Nov. 8, 2020.

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# VNE-Sim: simulation platform



S. Haeri and Lj. Trajković, "VNE-Sim: a virtual network embedding simulator,"  
in *Proc. SIMUTOOLS*, Prague, Czech Republic, Aug. 2016.  
<https://bitbucket.org/shaeri/vne-sim>



# Elements of DCN topologies

DCN Topology	Servers (hosts)	Switches (layer/level k)	Links
DCell(1,4)	20	5 (DCell <sub>0</sub> )	30
Bcube(2,4)	16	4 (BCube <sub>1</sub> ) 4 (BCube <sub>0</sub> )	32
Three-Tier	90	3 (core) 6 (aggregation) 18 (edge)	126
Spine-Leaf	90	6 (spine) 18 (leaf)	198
Collapsed Core	90	6 (spine) 18 (leaf)	123



# Parameters: substrate and virtual networks

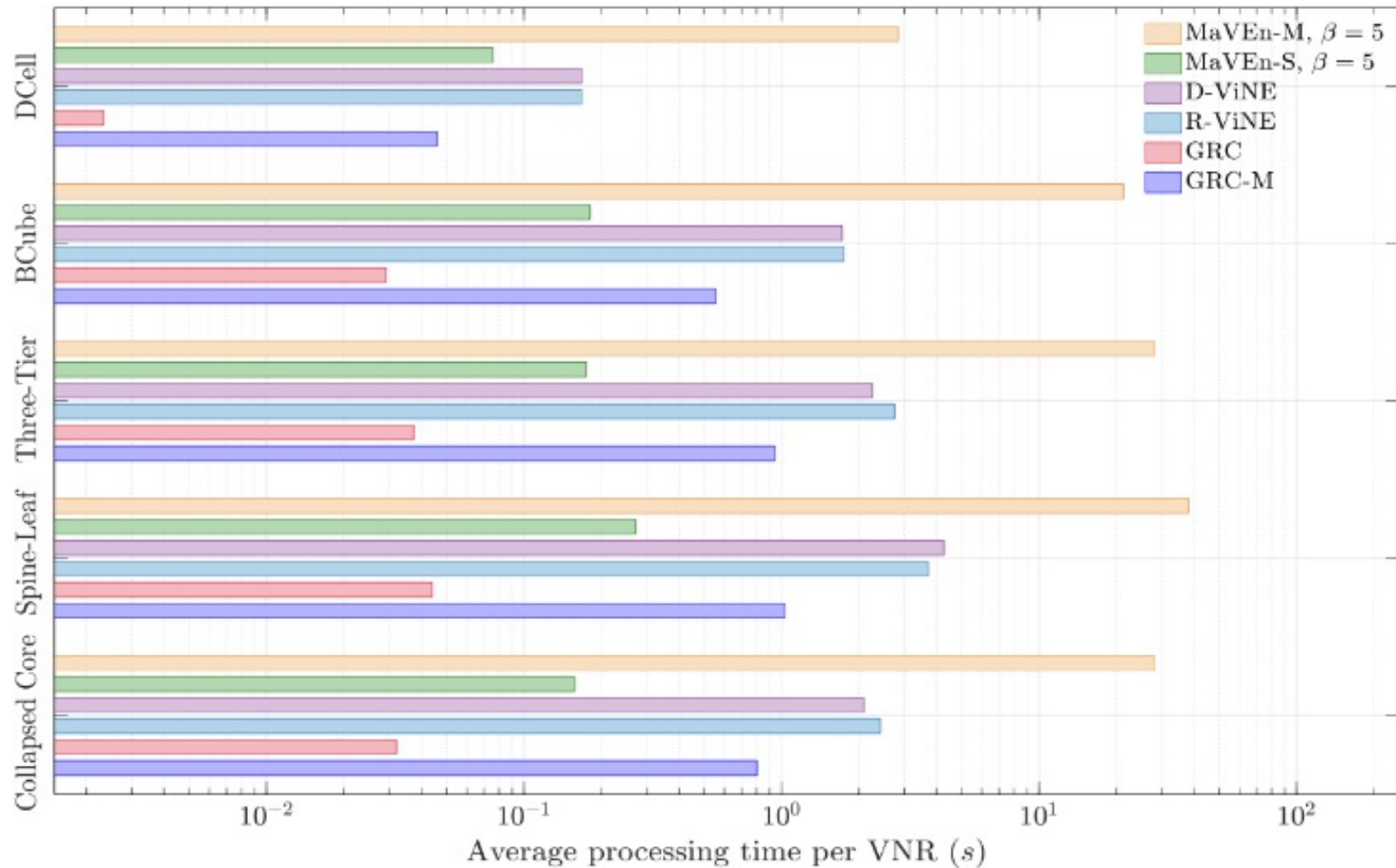
Parameter	Value and Distribution
SN CPU capacity	100 units
SN link bandwidth	100 units
Virtual CPU requirement	Uniformly distributed between 2 and 20 units
Virtual link bandwidth requirement	Uniformly distributed between 1 and 10 units
Link splitting rate	0.1
VNRs arrival	Poisson distribution with mean arrival rate $\lambda$ of requests per unit time
VNRs life-time	Exponentially distributed with a mean ( $\mu = 1,000$ )
VNRs traffic	$\lambda \times 1/\mu$ Erlangs

# Simulation parameters

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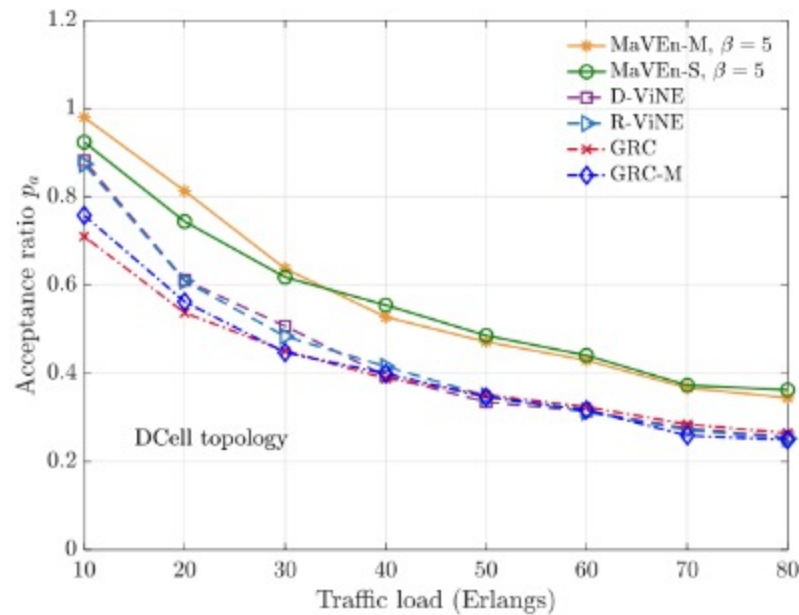
- Constant VNR arrival rate of 1 request per 100 time units:
  - traffic load of 10 Erlangs
- Duration of each scenario:
  - 50,000 time units
- Computational budget (number of simulations)  $\beta = 5$ :
  - number of evaluated action samples per selection cycle

# Average processing time

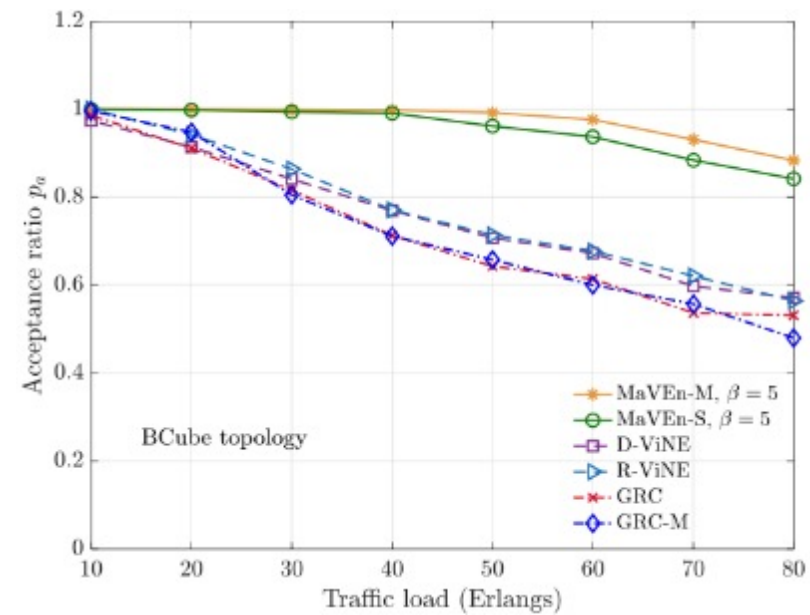


# Acceptance ratio: server-centric topologies

## DCell

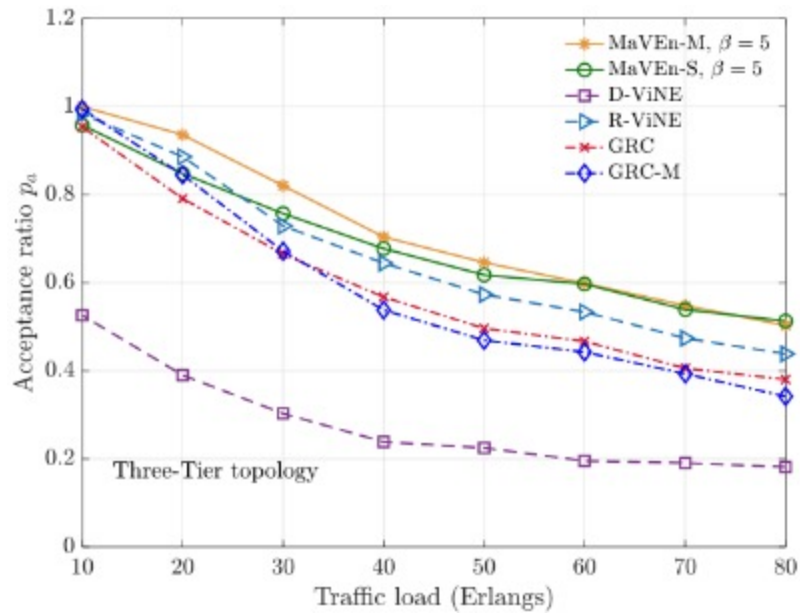


## BCube

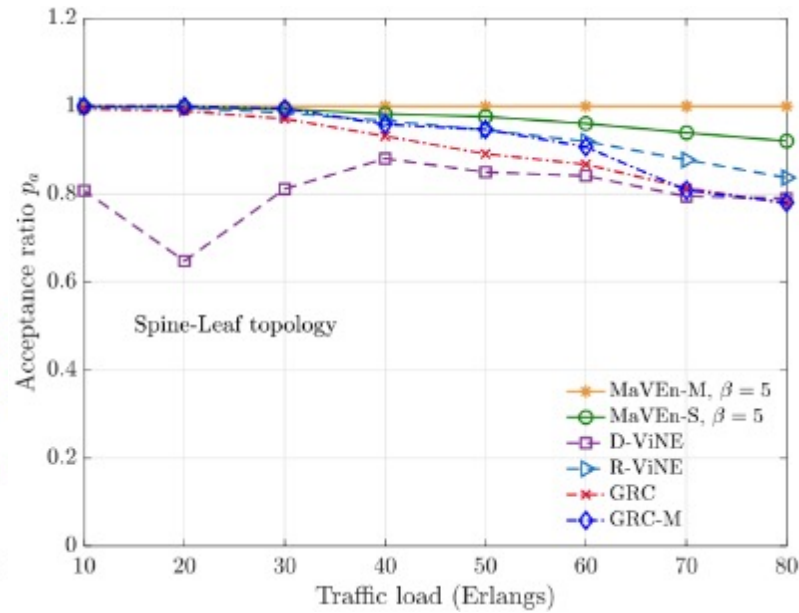


# Acceptance ratio: switch-centric topologies

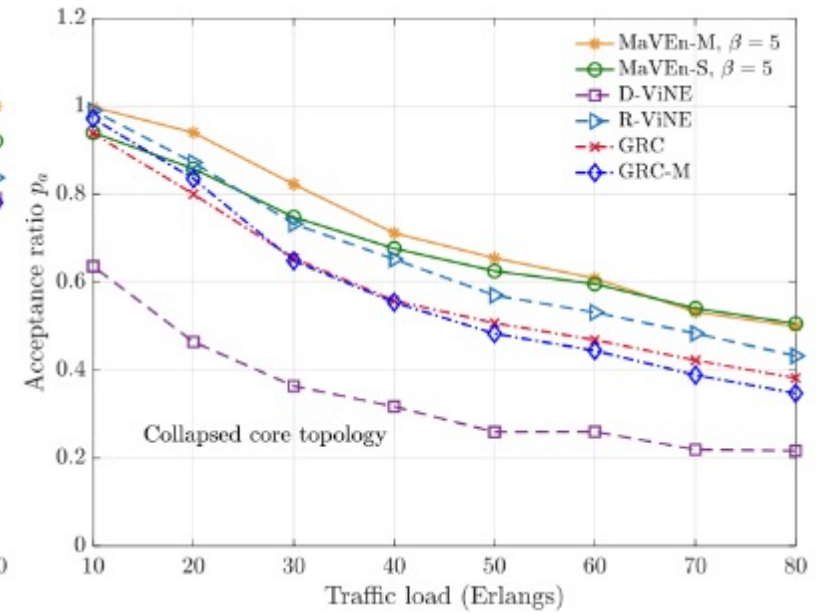
## Three-Tier



## Spine-Leaf

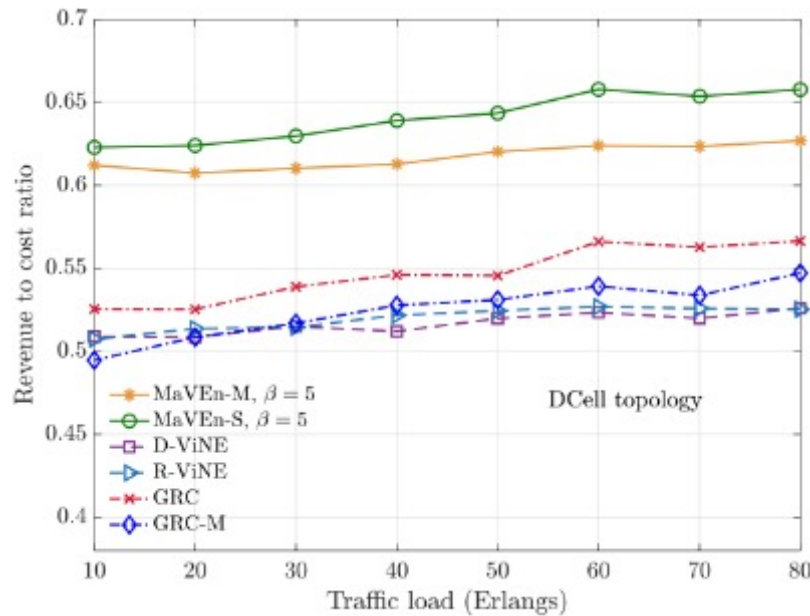


## Collapsed Core

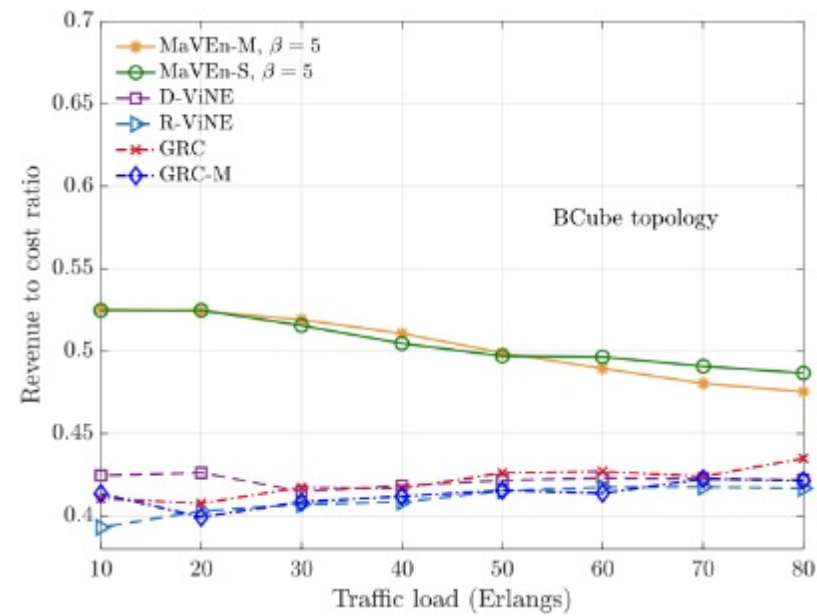


# Revenue to cost ratio: server-centric topologies

## DCell

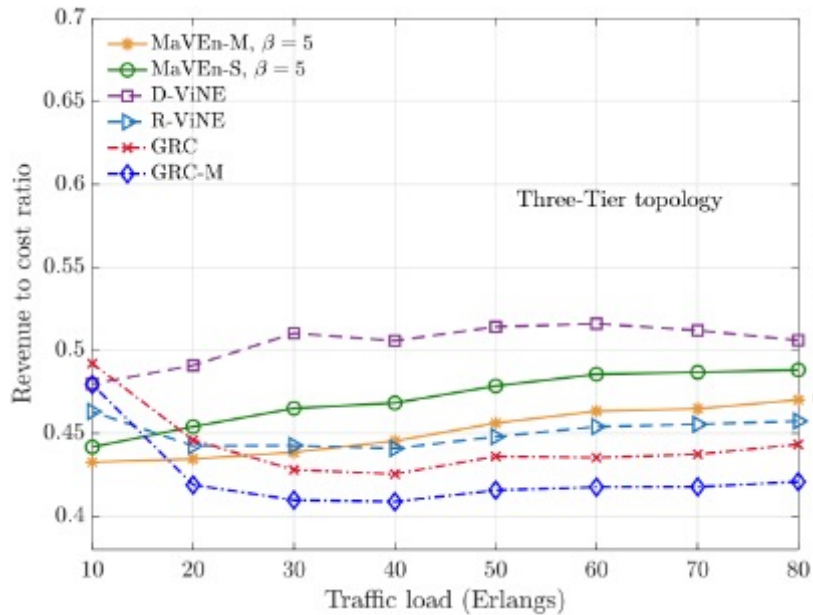


## BCube

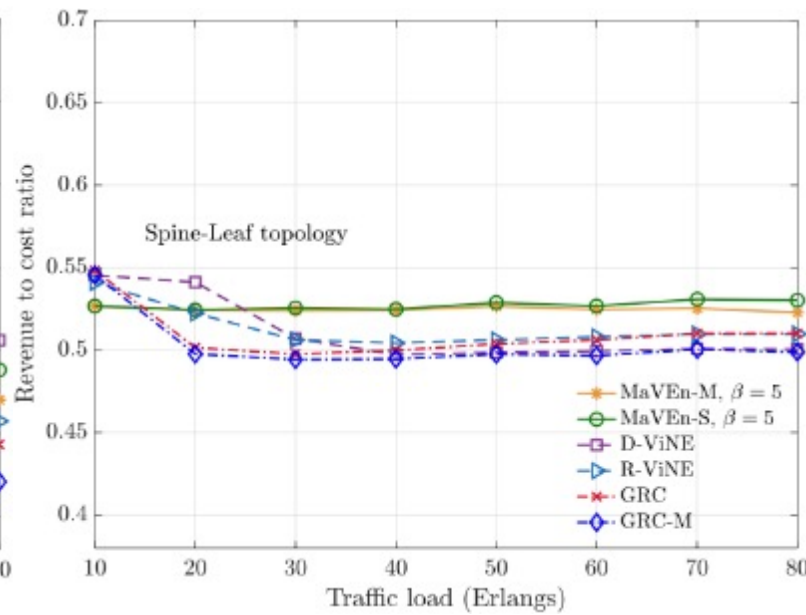


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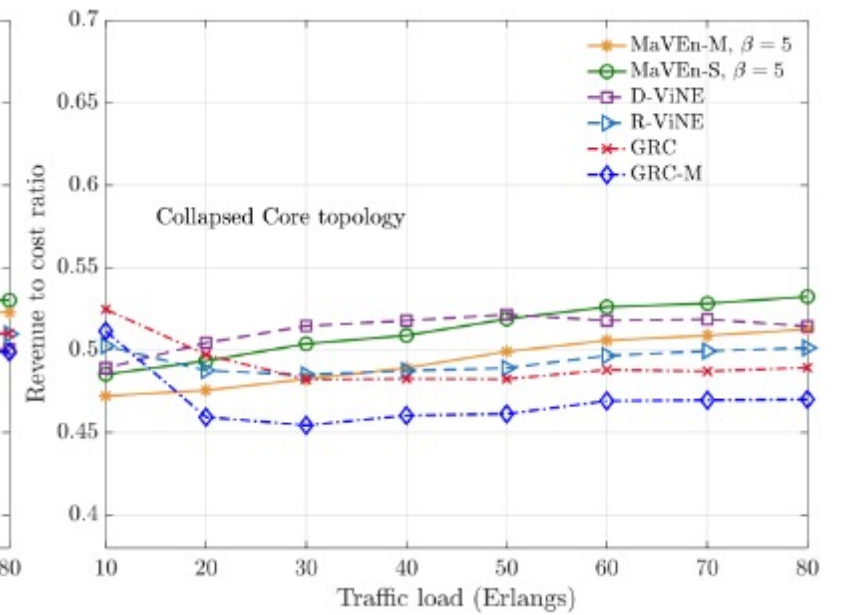
## Three-Tier



## Spine-Leaf

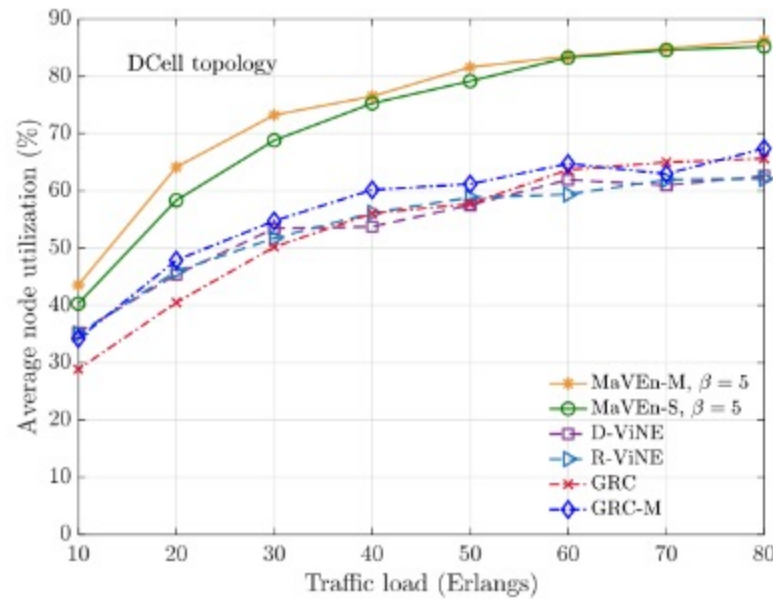


## Collapsed Core

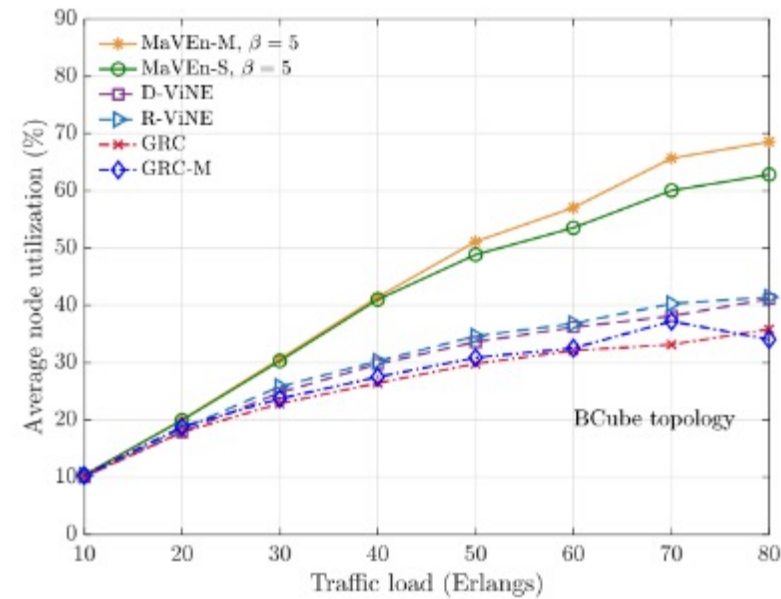


# Average node utilization: server-centric topologies

## DCell



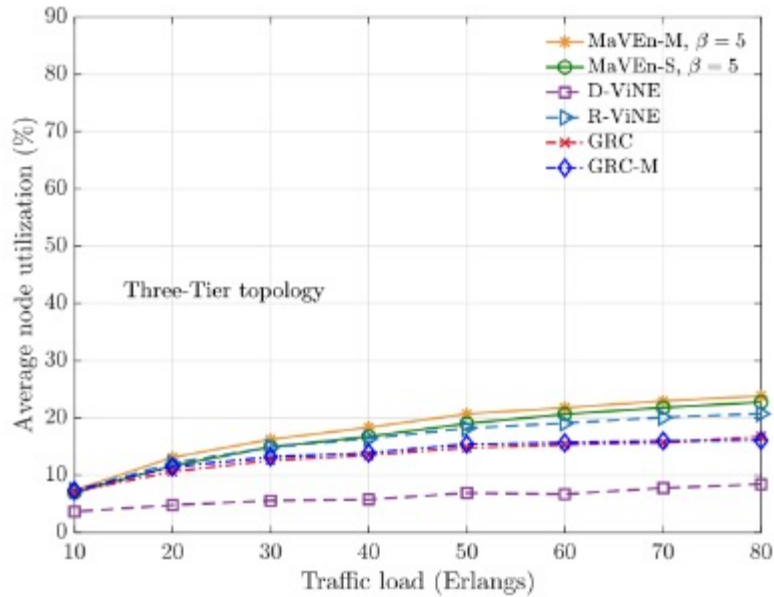
## BCube



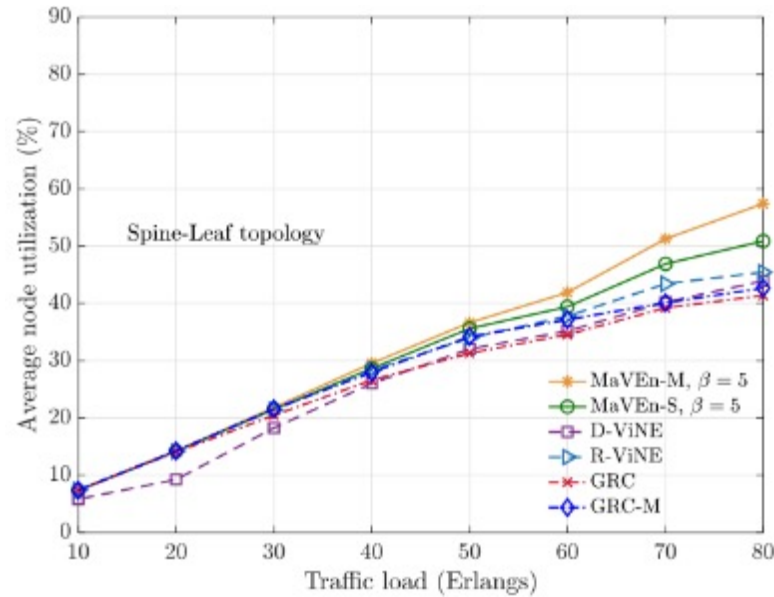


# Average node utilization: switch-centric topologies

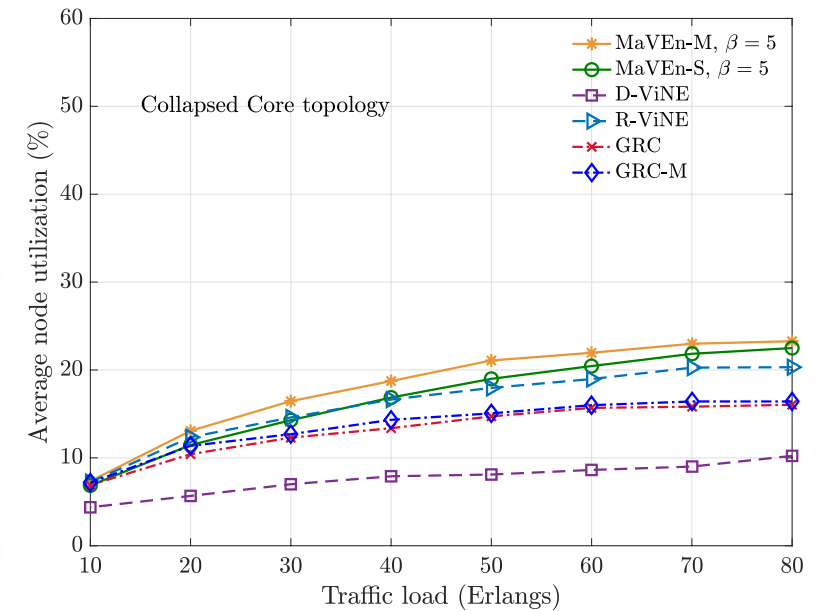
## Three-Tier



## Spine-Leaf

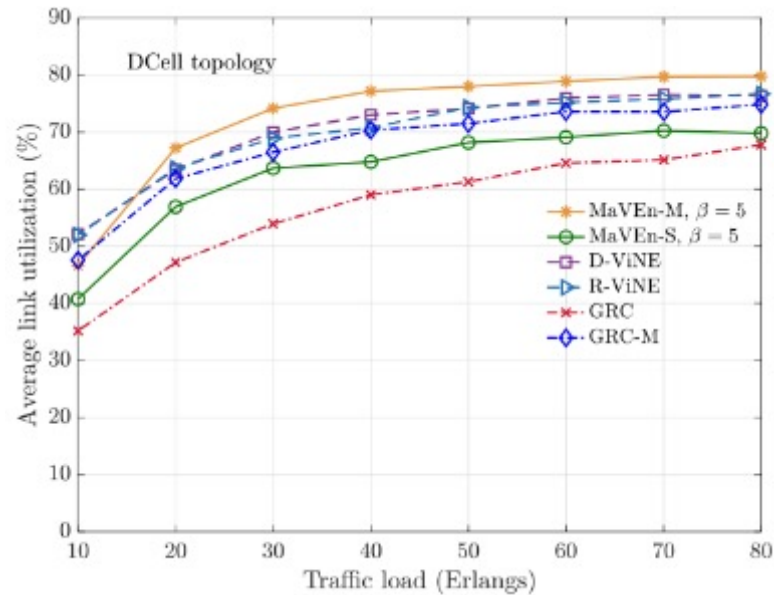


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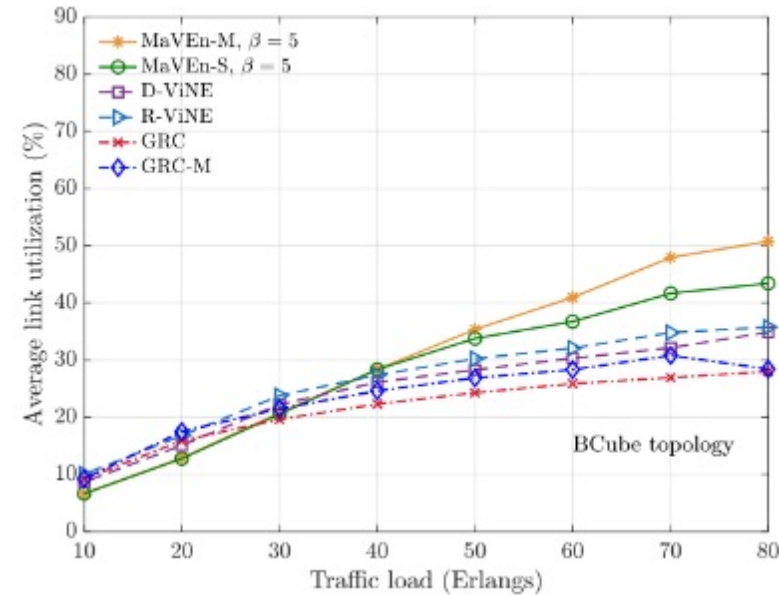


# Average link utilization: server-centric topologies

## DCell

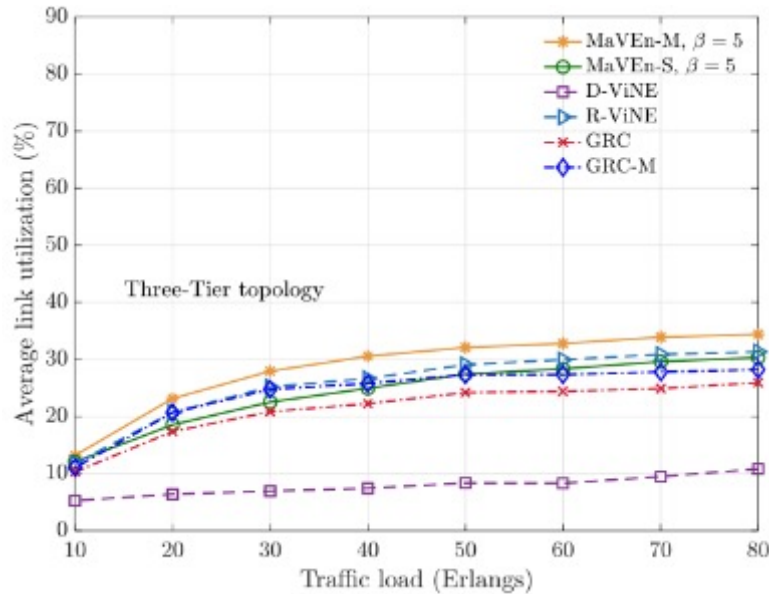


## BCube

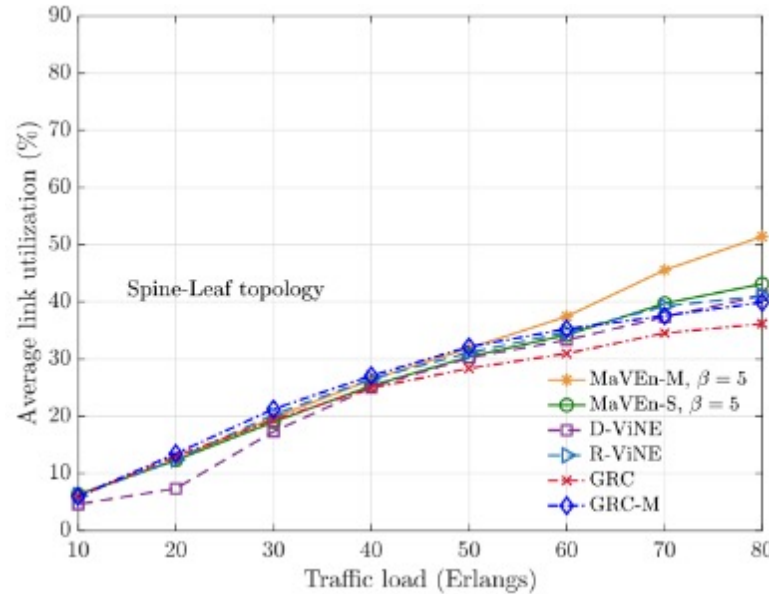


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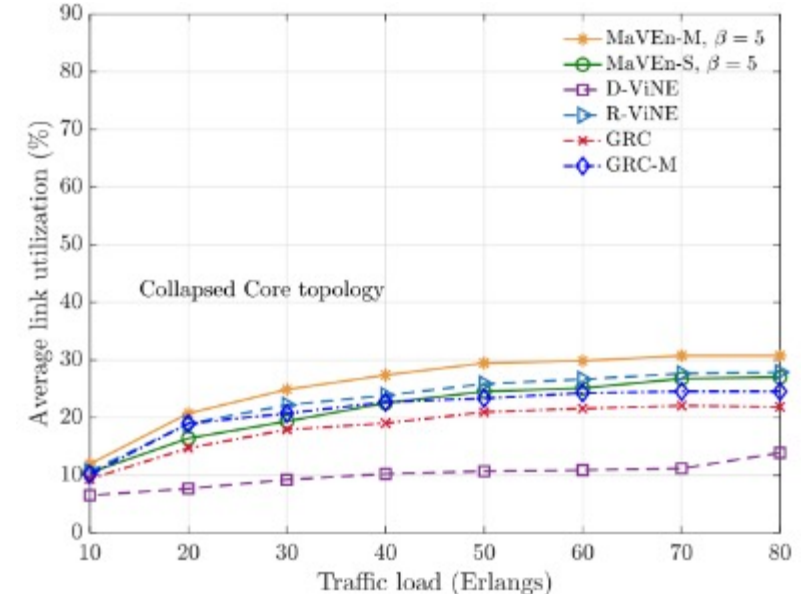
## Three-Tier



## Spine-Leaf



## Collapsed Core



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# Conclusion

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- We evaluated performance of:
  - MaVEn-M, MaVEn-S, D-ViNE, R-ViNE, GRC, and GRC-M VNE algorithms
  - DCell, BCube Spine-Leaf, Three-Tier, and Collapsed Core, data center network topologies
- GRC algorithm required the shortest processing time
- In most cases, MaVEn-M and MaVEn-S outperformed other algorithms due to their optimized embeddings
- Comparable performance was achieved using DCell:
  - fewer network elements than other DCN topologies
  - recursive connections between hosts

# References

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## Data Center Networks:

- M. Manzano, K. Bilal, E. Calle, and S. U. Khan, "On the connectivity of data center networks," *IEEE Commun. Lett.*, vol. 17, no. 11, pp. 2172–2175, Nov. 2013.
- W. Xia, P. Zhao, Y. Wen, and H. Xie, "A survey on data center networking (DCN): infrastructure and operations," *IEEE Commun. Surveys Tuts.*, vol. 19, no. 1, pp. 640–656, First Quarter 2017.

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- L. Gong, Y. Wen, Z. Zhu, and T. Lee, "Toward profit-seeking virtual network embedding algorithm via global resource capacity," in *Proc. IEEE INFOCOM*, Toronto, ON, Canada, Apr. 2014, pp. 1–9.

# References

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## Virtual Network Embedding Algorithms:

- A. L. Gonzalez Rios, K. Bekshentayeva, M. Singh, S. Haeri, and Lj. Trajković, "Virtual network embedding for switch-centric data center networks," in *Proc. IEEE Int. Symp. Circuits Syst.*, Daegu, Korea, May 2021 (virtual).
- S. Haeri and Lj. Trajković, "Virtual network embedding via Monte-Carlo tree search," *IEEE Trans. Cybern.*, vol. 47, no. 2, pp. 1–12, Feb. 2017.
- S. Haeri, Q. Ding, Z. Li, and Lj. Trajković, "Global resource capacity algorithm with path splitting for virtual network embedding," in *Proc. IEEE Int. Symp. Circuits and Systems*, Montreal, Canada, May 2016, pp. 666–669.
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- S. Haeri and Lj. Trajković, "Virtual network embeddings in data center networks," in *Proc. IEEE Int. Symp. Circuits and Systems*, Montreal, Canada, May 2016, pp. 874–877.